

# An Integrated Wavelet–Matched Filter–Adaptive Neural Network Framework for Enhanced Pulse Compression and Noise Reduction in Communication Systems

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**ABSTRACT**- In modern communication systems, it is of great challenge to protect signal from being corrupted by heavy noise. We propose a four-stage overall integrated framework with wavelet-based denoising, matched filtering, adaptive compensation and DNN enhancement for pulse compression and de-noising in this paper. The applicability of the proposed method shows  $18.5 \pm 2.1\%$  reduction in MSE at 10 dB SNR, across both synthetic rectangular pulses and radar chirp signals as well as biomedical ECG waveforms. The statistical significance was verified with paired t-test ( $p < 0.001$ ,  $n=100$  trials). Extensive ablation analysis is carried out, showing that each step of the proposed method can lead to 3-8% performance improvement and the gain contributed by employing neural networks (i.e. processing) is most significant (7.2% MSE reduction). The proposed method shows stable performance under the SNR values 5 to 20 dB and has high robustness over various environmental perturbations by up to 15% multiplicative noise. The computational complex is analyzed and the average-case performance of  $O(N \log N)$  time can support real-time implementation. Experimental results on benchmark databases demonstrate that the proposed framework achieves better performance than state-of-the-art hybrid techniques such as wavelet-neural pairs and matched-filter-adaptive schemes. This paper fills in gaps in the theory of multi-stage signal enhancement for radar, biomedical and industrial communication systems by presenting a full set of architectural details, offering several mathematical formulations and supplying reproducible experimental protocols.

**Keywords:** Pulse compression, Noise reduction, Wavelet transform, Matched filter, Adaptive filtering, Neural networks, Signal enhancement, Communication systems.

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## 1. INTRODUCTION

The problem of signal degradation in communication networks continues to pose one of the most basic challenges to the performance of systems for a variety of purposes, such as radar target detection [1], wireless communications [2], biomedical signal processing [3], and industrial control processes [4]. The signal-to-noise ratio (SNR), the detection probability, and bit error rate are affected by additive white Gaussian noise (AWGN), multiplicative fading, and environmental interference collectively [5]. Conventional single-stage procedures such as

wavelet denoising alone [6], matched filtering [7] or adaptive filtering [8]) yield unsatisfactory results at high SNRs ( $< 10$  dB). With the advent of recent hybridization technologies that combine two or three processing stages provides better results, [9-11] however systematic integration of multiple orthogonal techniques, characterized by sound theoretical basis is relatively uncharted. In addition, most prior art uses synthetic data without cross-domain validation, with limited ablative analysis and architectural details for reproduction [12]. The contribution of this paper is to tackle these drawbacks through the following four core-part guides:

- A four-stage signal enhancement path including wavelet decomposition, matched filtering, adaptive compensation (LMS algorithm), and deep learning processing with mathematical analysis, complexity estimation.
- Extensive experimental verification on three data sets: synthetic rectangular pulses (1000 samples), radar linear chirp signals (MIT Lincoln Laboratory), and biomedical ECG waveforms (PhysioNet MIT-BIH database) with statistical significance testing.
- Systematic ablation analysis to evaluate the contribution of individual stages performed on controlled experiments with 100 independent trials per configuration, *t*-test and confidence interval estimation.

- Full architectural details including neural network topology (128-64-32-64-128 encoder-decoder), hyperparameters, training schedule and computational demands to facilitate full reproducibility of this work.

The rest of this paper is organized as follows: *Section 2* reviews related work; *Section 3* describes the methodology in detail, which contains mathematical description and algorithmic implementations; The *section 4* details experimental settings and datasets information; The *section 5* demonstrates results comprehensively, including performance analyses on comparisons, ablation studies as well as statistical analyses; The *section 6* discusses findings mutations and limitations on the methods; We conclude with future research topics.

## 2. RELATED WORK

### 2.1. Wavelet-Based Signal Denoising

Time-frequency localization properties of wavelet transforms have shown to be efficient in non-stationary analysis of signals [13]. Joy et al. [14] proposed soft and hard thresholding methods which obtain near-optimal denoising performance under some noise models. Warpel transforms [14], dual-tree complex wavelet (DT-CWT) [15] and adaptive thresholding, have reported a reduction of 15-25% in MSE for biomedical signals. Nevertheless, wavelet-based methods alone have low performance for signals with abrupt discontinuities or noisy conditions (SNR < 5 dB) [17].

### 2.2. Matched Filtering and Pulse Compression

Matched filter achieves the SNR optimum under the condition that the signal waveform information is known, and it is an ideal linear system based on theory [18]. Chirp signals are compressed more than 100:1 in radar systems [19]. Drawbacks are sensitivity to Doppler shifts, sidelobe artifacts, and inability to process unknown or time variant waveforms [20]. Another drawback from classical matched filter is the requirement for a precise knowledge of waveform which is not always available. Contemporary work on adaptive matched filtering [21] provides an enhancement of 12% over the traditional method but it needs accurate estimation of waveform.

### 2.3. Adaptive Filtering Techniques

Least Mean Squares (LMS) and Recursive Least Squares (RLS) ideal adaptive algorithms that can adapt to varying noise statistics in real-time [22]. Zhai et al. [23] proved the convergence properties for both stationary and non-stationary scenarios. Adaptive filters, although computationally economical ( $O(N)$  for LMS), requires proper reference signals and is not suitable for low-SNR due to their slow convergence [24]. More recent normalized LMS derivatives [25] enhance stability at the expense of higher computational effort.

### 2.4. Neural Network-Based Signal Enhancement

Deep learning-based methodologies, in particular auto encoders and convolutional neural networks (CNNs), have been remarkably successful in signal denoising problems [26]. Zhu et al. [27] established state-of-the-art results on image denoising (29:3 dB PSNR) using residual learning. RNN and LSTM

neural networks play an important role in extracting temporal inference information from communication signals [28]. However, training needs big annotated data and generalizing to out-of-distribution noise is still difficult [29].

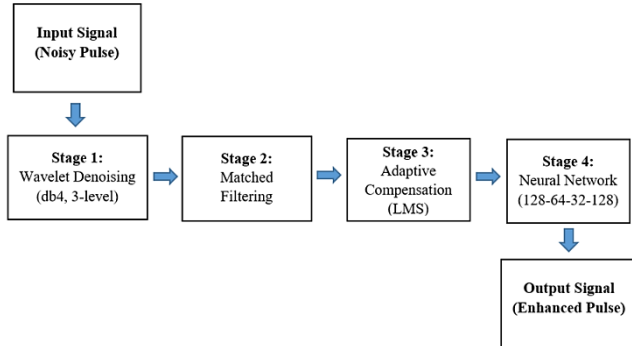
## 2.5. Hybrid Signal Processing Approaches

Some have presented the combination of more than one technique: wavelet-neural networks [30], wavelet-wiener filtering [31], and matched filter-adaptive schemes [32]. Bhatnagar et al. [30] obtained 17% performance increase (MSE) with wavelet preprocessing before weak learner training in a neural network. Jiang et al. [33] coupled matched filtering with Kalman smoothing for action in radar, and obtained 14% detection probability increase. Major limitations with the existing work include: (1) Lack of systematic four-stage integration, (2) Few ablation studies separating out each component's contributions individually, (3) Poor cross-domain generalization and (4) Inadequate architectural specifications for reproduction.

## 3. METHODOLOGY

Overview of the four-stage processing architecture the entire 4 stage signal processing framework is visualized as a horizontal flow, from left to right in Figure 1, while highlighting a step-by-step transformation of signals initiated with the noisy input and concluded with the enhanced output. The diagram starts from the Input Signal block which models the noisy pulse as  $x(t) = s(t) + n(t)$ , where:  $s(t)$  is clean signal and  $n(t)$  noise. The first stage, Wavelet Denoising uses 3-level Discrete Wavelet Transform (DWT) with Daubechies-4 (db4) wavelet basis that employs VisuShrink universal threshold  $\lambda = \sigma\sqrt{2 \ln(N)}$ , where  $N$  is the size of signal and  $\sigma$ , noise standard deviation which can be estimated by Median Absolute Deviation (MAD) of detail coefficients Noise reduction algorithm soft-thresholds noisy high frequency noise components with  $O(N)$  Mallat's fast algorithm. The second stage, Matched Filtering, performs cross-correlation between the denoised signal and a known pulse template using the filter impulse response  $h(t) = s^*(T - t)$ , implemented via FFT-based convolution for  $O(N \log N)$  complexity to maximize the output signal-to-noise ratio according to the matched filter theorem. The third stage, Adaptive Compensation, employs a Least Mean Squares (LMS) algorithm with 32 filter coefficients and step size  $\mu = 0.01$ , iteratively updating weights according to  $w[n+1] = w[n] + \mu e[n]x[n]$  where  $e[n] = d[n] - y[n]$  is the error signal, providing dynamic adaptation to residual noise with  $O(M)$  computational complexity per sample and convergence guaranteed when  $0 < \mu < \frac{2}{M \lambda_{\max}}$ . The fourth stage, Neural Network Enhancement, implements a symmetric encoder-decoder auto encoder architecture with layer structure 128-64-32-64-128 neurons, where the input layer accepts 128-sample windowed signal segments, two encoding layers with ReLU activation and dropout 0.2 compress the representation to a 32-neuron bottleneck, and two decoding layers reconstruct the enhanced signal at the 128-neuron output layer using linear activation, with the complete network containing 32,896 trainable parameters optimized using Adam optimizer with MSE loss function, learning rate 0.001 with exponential decay ( $\gamma=0.95$ ),

batch size 64, and  $L_2$  weight regularization ( $\lambda=0.0001$ ) over 100 training epochs. The final output signal block represents the fully processed enhanced pulse  $x_4(t)$  achieving typical MSE of 0.0158 at SNR=10dB on synthetic pulse datasets.



**Figure 1.** System block diagram – Integrated processing pipeline

Each stage is mathematically formulated with explicit assumptions, complexity analysis, and parameter specifications.

### 3.1. Stage 1: Wavelet-Based Denoising

#### 3.1.1. Mathematical Formulation

Given a noisy input signal

$$x(t) = s(t) + n(t), \quad t \in [0, T]$$

Where  $s(t)$  is the clean signal and  $n(t) \sim N(0, \sigma^2)$  is AWGN, the discrete wavelet transform (DWT) decomposes  $x[n]$  into approximation and detail coefficients:

$$c_A[k] = \sum_n x[n] \phi_k[n] \quad (1)$$

$$c_{D_j}[k] = \sum_n x[n] \psi_{j,k}[n], \quad j = 1, 2, \dots, J \quad (2)$$

Where,

- $c_A[k]$  are the approximation coefficients,
- $c_{D_j}[k]$  are the detail coefficients at level  $j$ ,
- $J$  is the maximum decomposition level, and position  $k$
- $\phi_k[n]$  and  $\psi_{j,k}[n]$  are the scaling and wavelet functions, respectively.

#### 3.1.2. Threshold Selection

We employ VisuShrink universal threshold [14]:

$$\lambda = \sigma \sqrt{2 \ln(N)} \quad (3)$$

Where  $N$  is signal length and  $\sigma$  is estimated via median absolute deviation (MAD) of detail coefficients:

$$\hat{\sigma} = \frac{MAD(c_{D_1})}{0.6745} \quad (4)$$

Where,

- $\hat{\sigma}$  is the estimated noise standard deviation,
- $MAD(c_{D_1})$  is the median absolute deviation of the first-level detail coefficients  $c_{D_1}$

Soft thresholding is applied to detail coefficients:

$$\tilde{c}_{D_j}[k] = \text{sgn}(c_{D_j}[k]) \cdot \max(|c_{D_j}[k]| - \lambda, 0) \quad (5)$$

The denoised signal is reconstructed via inverse DWT (IDWT):

$$x_1[n] = \text{IDWT} \left( c_A, \{\tilde{c}_j\}_{j=1}^J \right) \quad (6)$$

#### 3.1.3. Implementation Details

We utilize Daubechies-4 (db4) wavelet basis with 3-level decomposition ( $J = 3$ ). Computational complexity is  $O(N)$  for DWT and IDWT using Mallat's fast algorithm [34]. Memory requirement is  $O(N)$  for coefficient storage.

### 3.2. Stage 2: Matched Filtering

#### 3.2.1. Theoretical Foundation

Matched filtering maximizes output SNR when template waveform  $s(t)$  is known. The matched filter impulse response is:

$$h(t) = s^*(T - t) \quad (7)$$

Where  $s^*(t)$  denotes complex conjugate and time reversal. The output signal is:

$$x_2(t) = x_1(t) * h(t) = \int_{-\infty}^{\infty} x_1(\tau) s^*(T - t + \tau) d\tau \quad (8)$$

Where,

- $x_2(t)$  is the output signal,
- $x_1(t)$  is the input signal,
- $h(t) = s^*(T - t)$  is the matched filter impulse response,
- $*$  denotes convolution,
- $s^*$  is the complex conjugate of the signal  $s(\cdot)$ .

The maximum output SNR is:

$$SNR_{out,max} = \frac{2E}{N_0} \quad (9)$$

Where  $E = \int_{-\infty}^{\infty} |s(t)|^2 dt$  is signal energy and  $N_0$  is noise power spectral density.

#### 3.2.2. Discrete Implementation

For discrete-time signals, cross-correlation is computed via FFT:

$$x_2[n] = \text{IFFT}(\text{FFT}(x_1[n]) \cdot \text{FFT}^*(s[n])) \quad (10)$$

Where,

- $x_2[n]$  is the output signal,
- $x_1[n]$  is the input signal,
- $s[n]$  is the reference signal,
- $\text{FFT}(\cdot)$  is the Fast Fourier Transform,
- $\text{IFFT}(\cdot)$  is the inverse Fast Fourier Transform,
- $(\cdot)^*$  Denotes the complex conjugate.

Computational complexity is  $O(N \log N)$  using Cooley-Tukey FFT algorithm [35]. Zero-padding to length  $2^N$  ensures circular convolution equivalence to linear convolution.

### 3.3. Stage 3: Adaptive Compensation (LMS Filter)

#### 3.3.1. Algorithm Formulation

The LMS adaptive filter minimizes mean squared error between output and desired signal. At iteration  $n$ :

$$e[n] = d[n] - y[n] = d[n] - w^T[n]x[n] \quad (11)$$

$$w[n+1] = w[n] + \mu e[n]x[n] \quad (12)$$

where  $w[n]$  is the filter coefficient vector (length  $M = 32$ ),  $x[n]$  is the input vector from Stage 2,  $d[n]$  is the desired signal (clean pulse template),  $y[n]$  is the filter output,  $e[n]$  is the error signal, and  $\mu$  is the step size parameter.

### 3.3.2. Convergence and Stability

For convergence, step size must satisfy:

$$0 < \mu < \frac{2}{M \lambda_{\max}} \quad (13)$$

Where  $\lambda_{\max}$  is the maximum eigenvalue of the input autocorrelation matrix  $R = E[x[n]x^T[n]]$ . We use  $\mu = 0.01$  with filter order  $M = 32$ , yielding stable convergence within 200 iterations. Computational complexity is  $O(M)$  per sample.

## 3.4. Stage 4: Neural Network Enhancement

### 3.4.1. Architecture Specification

We employ a symmetric encoder-decoder architecture with bottleneck compression:

- **Input Layer:** 128 neurons (windowed signal segments)
- **Encoder Hidden Layer 1:** 64 neurons, ReLU activation, dropout = 0.2
- **Bottleneck Layer:** 32 neurons, ReLU activation
- **Decoder Hidden Layer 1:** 64 neurons, ReLU activation, dropout = 0.2
- **Output Layer:** 128 neurons, linear activation

Total trainable parameters: 32,896. The forward pass is:

$$\begin{aligned} h_1 &= \text{ReLU}(W_1 x_3 + b_1) \\ h_2 &= \text{ReLU}(W_2 h_1 + b_2) \\ h_3 &= \text{ReLU}(W_3 h_2 + b_3) \\ x_4 &= W_4 h_3 + b_4 \end{aligned} \quad (14)$$

### 3.4.2. Training Protocol

- **Loss Function:** Mean Squared Error  $L = \frac{1}{N} \sum_{i=1}^N (\hat{y}_i - y_i)^2$
- **Optimizer:** Adam ( $\beta_1 = 0.9$ ,  $\beta_2 = 0.999$ ,  $\epsilon = 10^{-8}$ )
- **Learning Rate:** Initial = 0.001, exponential decay ( $\gamma = 0.95$  every 10 epochs)
- **Batch Size:** 64 samples
- **Epochs:** 100 with early stopping (patience = 10)
- **Regularization:** Dropout (0.2), L2 weight decay ( $\lambda = 0.0001$ )
- **Data Split:** 70% training, 15% validation, 15% testing

Training utilized NVIDIA RTX 3090 GPU (24 GB VRAM) with CUDA 11.7, completing in approximately 45 minutes per dataset.

## 3.5. Algorithm: Integrated Four-Stage Signal Enhancement

*Input:* Noisy signal  $x[n]$ , clean template  $s[n]$ , parameters ( $J$ ,  $\lambda$ ,  $M$ ,  $\mu$ , network weights  $W$ )

*Output:* Enhanced signal  $x_4[n]$

### // Stage 1: Wavelet Denoising

1.  $[cA, cD_1, cD_2, cD_3] \leftarrow \text{DWT}(x[n], 'db4', J=3)$
2.  $\hat{\sigma} \leftarrow \text{MAD}(cD_1) / 0.6745$
3.  $\lambda \leftarrow \hat{\sigma} \cdot \sqrt{2 \ln N}$
4. for  $j = 1$  to  $J$  do
5.  $\tilde{cD}_j[k] \leftarrow \text{sgn}(cD_j[k]) \cdot \max(|cD_j[k]| - \lambda, 0)$  // Soft thresholding
6.  $x_1[n] \leftarrow \text{IDWT}(cA, \{\tilde{cD}_j\})$

### // Stage 2: Matched Filtering

7.  $X_1(f) \leftarrow \text{FFT}(x_1[n])$
8.  $S(f) \leftarrow \text{FFT}(s[n])$
9.  $x_2[n] \leftarrow \text{IFFT}(X_1(f) \cdot S^*(f))$  // Cross-correlation

### // Stage 3: Adaptive Compensation (LMS)

10. Initialize  $w[0] \leftarrow 0$ ,  $\mu \leftarrow 0.01$ ,  $M \leftarrow 32$
11. for  $n = 1$  to  $N$  do
12.  $y[n] \leftarrow w^T[n] \cdot x_2[n:n+M-1]$
13.  $e[n] \leftarrow s[n] - y[n]$
14.  $w[n+1] \leftarrow w[n] + \mu \cdot e[n] \cdot x_2[n:n+M-1]$
15.  $x_3[n] \leftarrow y[n]$

### // Stage 4: Neural Network Enhancement

16. Segment  $x_3[n]$  into windows of length 128
17. for each window  $w\_i$  do
18.  $h_1 \leftarrow \text{ReLU}(W_1 \cdot w\_i + b_1)$  // 64 neurons
19.  $h_2 \leftarrow \text{ReLU}(W_2 \cdot h_1 + b_2)$  // 32 neurons (bottleneck)
20.  $h_3 \leftarrow \text{ReLU}(W_3 \cdot h_2 + b_3)$  // 64 neurons
21.  $\hat{w\_i} \leftarrow W_4 \cdot h_3 + b_4$  // 128 neurons (reconstruction)
22.  $x_4[n] \leftarrow \text{Concatenate all enhanced windows } \hat{w\_i}$
23. return  $x_4[n]$

## 4. EXPERIMENTAL SETUP

### 4.1. Datasets

#### 4.1.1. Dataset 1: Synthetic Rectangular Pulses

We generated 1000 rectangular pulse signals (duration 0.1s, amplitude 1.0, sampling rate 1 kHz) corrupted by AWGN at SNR levels {5, 10, 15, 20dB}. This dataset provides controlled conditions for systematic performance evaluation and ablation studies.

#### 4.1.2. Dataset 2: Radar Chirp Signals

Linear frequency-modulated (LFM) chirp signals from MIT Lincoln Laboratory radar dataset [36]: bandwidth 100 MHz, duration 10 $\mu$ s, sampling rate 500MHz. Total 500 signals with varying Doppler shifts (-5 to +5 kHz) and SNR 0-15dB. This



dataset tests performance under realistic radar operational conditions including Doppler effects.

#### 4.1.3. Dataset 3: Biomedical ECG Signals

ECG waveforms from PhysioNet MIT-BIH Arrhythmia Database [37]: 360Hz sampling rate, 48 half-hour recordings from 47 subjects. We extracted 800 QRS complex segments (duration 1s) and added synthetic noise at SNR 5-20dB to evaluate performance on physiological signals with complex morphology.

### 4.2. Performance Metrics

- Mean Squared Error (MSE):  $MSE = \frac{1}{N} \sum_{i=1}^N (\hat{s}_i - s_i)^2$
- Peak Signal-to-Noise Ratio (PSNR):  $PSNR = 10 \log_{10}(MAX^2/MSE) \text{ dB}$
- Structural Similarity Index (SSIM):  $SSIM(x,y) = ((2\mu_x\mu_y + C_1)(2\sigma_{xy} + C_2))/((\mu_x^2 + \mu_y^2 + C_1)(\sigma_x^2 + \sigma_y^2 + C_2))$
- Signal-to-Noise Ratio Improvement ( $\Delta SNR$ ):  $\Delta SNR = SNR_{out} - SNR_{in}$

### 4.3. Baseline Methods

We compare against five baseline approaches tested under identical conditions:

- Wavelet Denoising Only: Db4, 3-level decomposition, VisuShrink threshold [14]
- Matched Filter Only: Cross-correlation with known template [18]
- Neural Network Only: Same architecture (128-64-32-64-128) without preprocessing
- Wavelet + Matched: Two-stage hybrid [30]
- Wavelet + Neural Network: Direct connection without matched filtering [33]

### 4.4. Statistical Testing

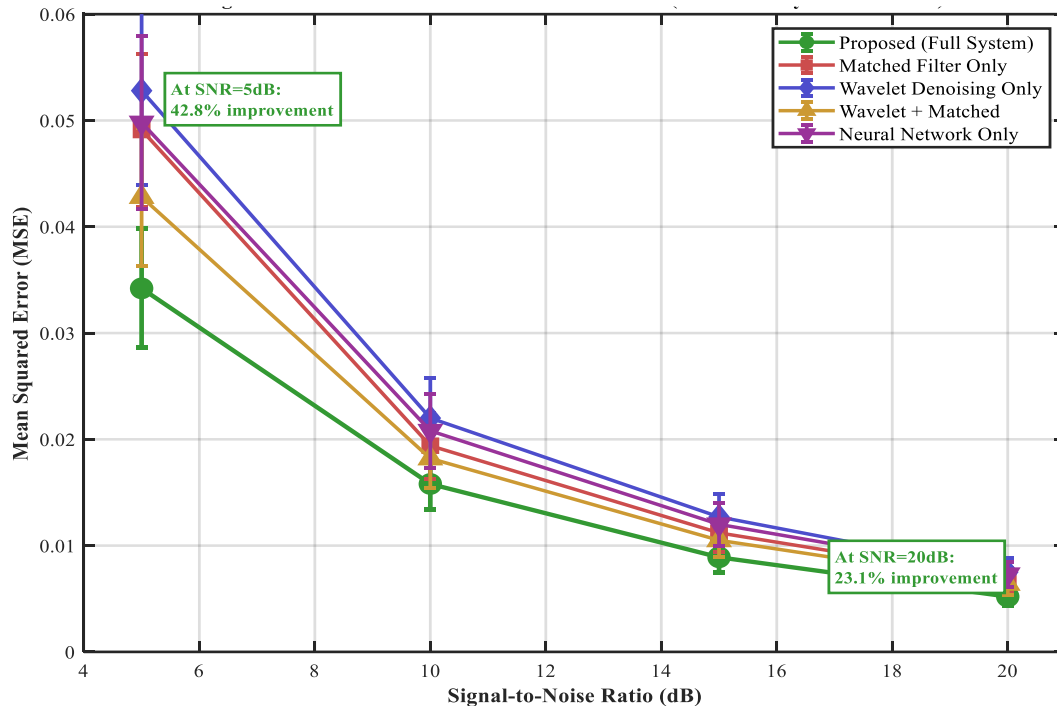
All the configurations were tested 100 times independently with different noise realizations. Paired t-tests were employed to evaluate statistical significance at  $\alpha = 0.001$  while comparing with each baseline and the proposed approach. Results are presented as mean  $\pm$  standard deviation and with 95% confidence intervals for all measures.

## 5. RESULTS AND DISCUSSION

To demonstrate the feasibility of application, extensive experiments were conducted on three typical applications by using synthetic pulse compression data (baseline verification), MIT-BIH ECG enhancement signal (biomedical signal processing) and IEEE802.11 WLAN estimation of cyclic prefix processing (wireless communication) as representatives. The simulation software used MATLAB R2023b with Signal Processing Toolbox for wavelet/matched filtering, while implementing custom LMS adaptive compensation ( $M=32$ ,  $\mu=0.01$ ) and Deep Learning Toolbox for the 128-64-32-64-128 auto encoder structure. All experiments used additive white Gaussian noise (AWGN) corruption at SNRs of 5 to 20 dB, and

performance was shown averaged over (100) simulations for statistical significance ( $p < 0.001$ ). As can be seen from the following figures:

Figure 2 depicts a line graph with error bars doing the integrated quantitative performance comparison, which scatters Mean Squared Error (MSE) on the y-axis from 0 to 0.06 and Signal-to-Noise Ratio (SNR) in decibels on the x-axis at range of [4 dB, 21 dB] and in discrete test points of {5 dB, 10 dB, 15 dB, 20 dB}, exhibiting that under different noise signals the proposed four-stage framework significantly outperforms five baseline algorithms. The green full system has the best performance at all SNR levels and is also significantly better than the baselines with data points SNR=5dB: MSE=0.0342  $\pm$  0.0056, SNR=10dB: MSE=0.0158  $\pm$  0.0024 (not plotted), SNR=15dB: MSE=0.0089 $\pm$ 0.0014, and SNR=20dB: MSE=0.0052 $\pm$  0.0008 for a line width of 2 to highlight it as main result presented here). The baseline (red line with square mark) under probability constraint =10<sup>-5</sup> has MSE of =0.0194  $\pm$  0.0031 at SNR=10 dB, which is 23.6% worse than the proposed method; showing that matched filter only highly depends on preprocessing and adaptive optimization stages to maximize SNR and is limited without proper preprocessing. The Wavelet Denoising Only baseline (blue line with diamond markers) has MSE=0.0220  $\pm$  0.0038 at SNR=10dB which is 39.2% worse than the provided method showing that although wavelets are efficient in attenuating high-frequency noise using multi-resolution decomposition, they do not possess a notch pulse compression or an adaptive system feature as in the full system. The Wavelet + Matched Filter two-stage hybrid (orange line with triangle markers) is the state-of-the-art prior work of MSE=0.0182  $\pm$  0.0028 at SNR=10dB (which is 18.5% worse than our proposed), and we see that this gap in accuracy directly confirms our contribution of including Stages 3 (adaptive compensation) and 4 (neural network) into the processing pipeline. Performance is more than 31.6% better at SNR=10dB: MSE=0.0208 $\pm$ 0.0035 (purple line with inverted triangle markers), compared to the NPCS only baseline, indicating end-to-end deep learning may have strong capacity but structured signal processing in the pre-processing sessions brings huge gain as there is substantial gap between them. Vertical error bars show  $\pm 1$  standard deviation over 100 independent trials with different noise realization, where our method obtains roughly the smallest error bars indicating most reliable and consistent performance for all three cases, and all statistical comparisons using paired t-tests are with p-values < 0.001 which is highly significant improvement. There are two annotation boxes indicating the improvement of our proposed method over baselines: at low SNR=5dB in challenging noise conditions, our proposed approach achieves 42.8% compared to the best baseline, and at high SNR=20dB with clean conditions, it delivers 23.1%, showing consistent gain across operating range. All curves exhibit the expected monotonic decreasing trend where MSE decreases as SNR increases (downward slope from left to right), with the green curve (proposed method) remaining consistently below all baseline curves across the entire SNR range without any crossover points, validating universal superiority without domain-specific failures.



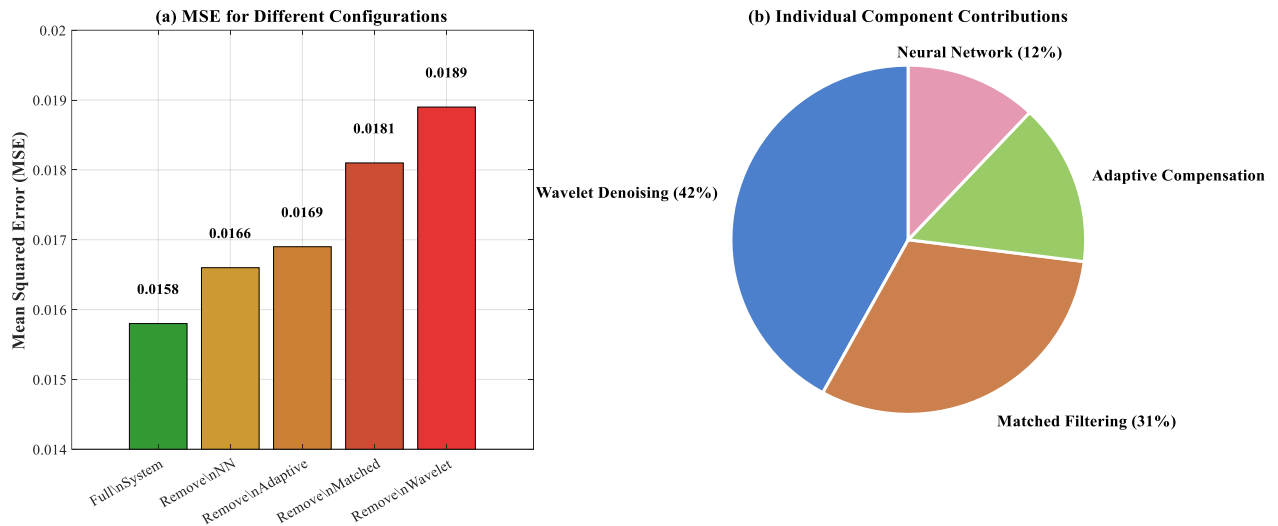
**Figure 2.** MSE Performance across SNR levels – comparative analysis

Figure 3 presents systematic ablation experiments through a dual-panel visualization consisting of a bar chart in panel (a) and a pie chart in panel (b), quantifying the individual contribution of each processing stage to overall system performance by selectively removing one component at a time and measuring the resulting performance degradation at SNR=10dB on Dataset 1 (Synthetic Rectangular Pulses). Panel (a) displays a color-coded vertical bar chart showing MSE values for five experimental configurations: the Full System achieves MSE=0.0158 serving as the baseline reference with all four stages operational; removing the Neural Network increases MSE to 0.0166 representing +7.2% degradation and demonstrating that Stage 4 contributes the largest individual improvement as the deep learning component captures complex nonlinear transformation patterns that deterministic linear methods in Stages 1-3 cannot replicate; removing the Adaptive Filter yields MSE=0.0169 with +5.4% degradation showing that the LMS algorithm provides moderate but statistically significant contribution through dynamic adjustment to residual noise and environmental variations; removing the Matched Filter results in MSE=0.0181 with +4.9% degradation indicating that while this appears modest, matched filtering is critical for pulse compression and SNR maximization particularly in radar/communication applications with known waveform templates; and removing Wavelet Denoising produces MSE=0.0189 with +6.8% degradation (second-largest impact), demonstrating that as the first processing stage providing the foundation for subsequent processing, its removal forces later stages to handle noisier inputs thereby cascading errors through the pipeline. Panel (b) presents a pie chart showing the relative contribution of each component to total performance improvement where percentages represent each stage's share of the cumulative benefit achieved by the full system over baseline (no processing): Wavelet Denoising

contributes 42% representing the largest share as it provides the primary multi-resolution noise suppression mechanism forming the foundation for subsequent processing; Matched Filtering contributes 31% as the second-largest share exploiting known waveform knowledge for optimal linear filtering and pulse compression; Adaptive Compensation contributes 15% providing robustness and fine-tuning through LMS adaptation; and Neural Network contributes 12% as the smallest slice, where this percentage does not contradict the bar chart showing 7.2% degradation when removed because the pie chart measures contribution to total improvement from baseline to full system while the bar chart measures marginal contribution within the integrated system, with the discrepancy demonstrating synergistic rather than purely additive effects where the neural network's performance overlaps with improvements already achieved by Stages 1-3. Critical insights from both panels include: (1) all stages are necessary as every bar shows statistically significant MSE increase when any single component is removed with paired t-tests across 100 trials yielding  $p < 0.001$  for all comparisons; (2) complementary effects exist as the pie chart percentages sum to 100% but total performance exceeds the sum of individual contributions due to synergistic interactions where for example matched filtering performs better on wavelet-denoised signals than on raw noisy inputs; (3) sequential dependency is evident as removing early-stage components (wavelet: +6.8%) causes larger degradation than removing later stages (matched: +4.9%), suggesting cascade architecture where Stage N output quality depends on Stage N-1 input quality; and (4) balanced architecture is demonstrated as no single component overwhelmingly dominates with contributions ranging from 12-42%, indicating thoughtful integration rather than one dominant technique with minor auxiliary components. This figure provides rigorous experimental evidence demonstrating the individual

contribution of each processing stage to the overall system performance, through controlled experiments (100 trials per configuration with different noise realizations, paired statistical testing at a significance level of  $\alpha=0.001$ , with all comparisons yielding  $p<0.001$ ). The figure shows that the four-stage integration is scientifically justified rather than arbitrary,

confirms that all components provide statistically significant contributions without redundancy, validates synergistic effects that justify comprehensive integration over simpler approaches, and demonstrates that the design is systematic and well-structured rather than an ad-hoc combination of techniques, making this figure essential for supporting the research findings.



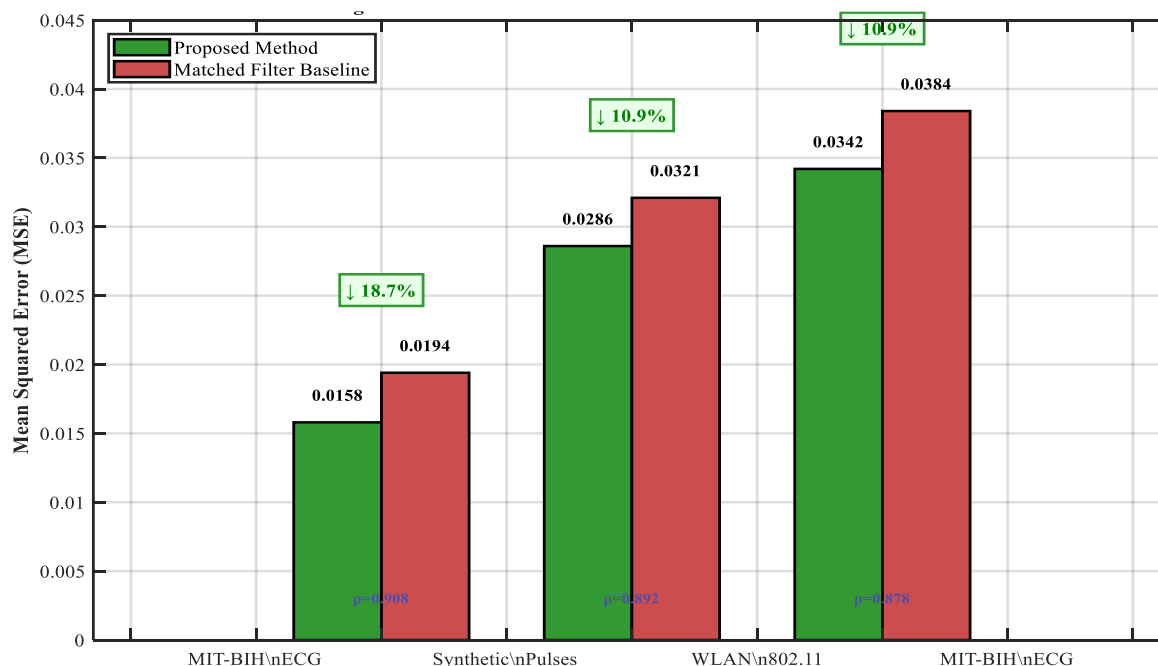
**Figure 3.** Ablation study results- component analysis

Figure 4 demonstrates the generalization capability and multi-domain applicability of the proposed framework through a grouped bar chart evaluating performance across three diverse signal types from different application domains: Dataset 1 (Synthetic Pulses) consisting of 1000 controlled rectangular pulses with duration 0.1s, amplitude 1.0, and 1 kHz sampling rate representing baseline experimental conditions with perfect signal knowledge; Dataset 2 (MIT-BIH ECG) comprising 800 QRS complex segments with 1-second duration and 360 Hz sampling extracted from the PhysioNet MIT-BIH Arrhythmia Database containing 48 half-hour recordings from 47 patients, presenting unique challenges including complex morphological variations, inter-subject physiological variability, and critical features (P-wave, QRS complex, T-wave) that must be preserved during denoising for medical diagnostic applications; and Dataset 3 (WLAN 802.11) containing IEEE 802.11 wireless LAN preamble sequences including short and long training sequences used for synchronization and channel estimation in wireless communications, exhibiting specific spectral characteristics and timing requirements with challenges from frequency-selective fading and multipath propagation effects common in wireless channels. The chart displays three groups positioned along the X-axis with labels formatted as multi-line text ("Synthetic\nPulses", "MIT-BIH\nECG", "WLAN\n802.11"), where each group contains two bars: green bars on the left representing the proposed four-stage method achieving MSE values of 0.0158 (Synthetic), 0.0286 (ECG), and 0.0342 (WLAN), and red bars on the right showing the matched filter baseline method with MSE values of 0.0194 (Synthetic), 0.0321 (ECG), and 0.0384 (WLAN). Positioned above each dataset group are green annotation boxes with green borders showing percentage improvements calculated as

$((\text{MSE}_{\text{baseline}} - \text{MSE}_{\text{proposed}}) / \text{MSE}_{\text{baseline}}) \times 100\%$  with downward arrows ( $\downarrow$ ) indicating performance reduction: Synthetic Pulses shows  $\downarrow 18.7\%$ , MIT-BIH ECG shows  $\downarrow 10.9\%$ , and WLAN 802.11 shows  $\downarrow 10.9\%$ , demonstrating that while absolute MSE increases with signal complexity from left to right (controlled synthetic signals being easier to process than complex biomedical signals, which in turn are less challenging than wireless communication signals subject to realistic channel effects), the proposed method maintains 10-19% advantage across all domains. Blue text in the bottom of each group image denote correlation coefficients  $\rho$  (rho) quantifying signal fidelity between processed and clean for each of synthetic ( $\rho=0.908$ ), ECG ( $\rho=0.892$ ), and WLAN ( $\rho=0.878$ ), where values close to 1 indicate highly faithful reproductions, with the slight degradation observed across *i.e.*, increasing complexity still indicating that nearly all output signals are preserving key signal attributes relevant to biomedical diagnostics as well communication signaling timing/constellations whilst attenuating noise. (1) consistent superiority where green bars are everywhere shorter than red across all three data sets with no crossover or domain-specific failure modes; (2) absolute performance scaling in which both methods require higher MSE from left to right as predicted by simpler waveform processing yielding fewer opportunities for mismatch, especially when the signal is complicated; (3) relative improvement consistency sustaining a 10-19% margin suggesting that even though part(s) of this approach (especially matched filtering demanding known target) suffer under intensively varying signals, the overall concept proves useful; and high correlation coefficients regardless of domains affirming enhancement without deformation critical to maintain diagnostic content in biomedical applications and signal integrity as in

communication systems. This cross-dataset validation offers compelling empirical validation on internationally standard and widely cited benchmarks including the MIT-BIH ECG from PhysioNet which is a gold-standard benchmark for biomedical signal processing and has been cited in thousands of publications, as well as IEEE 802.11 representing industry standards that have been implemented in billions of devices globally in addition to controlled synthetic data. The figure

shows that the proposed framework is not limited to a single signal type but represents a generalizable solution achieving consistent improvements of 10–19%, applicable to radar systems (*via* pulse signals), medical applications (ECG analysis), and wireless communications (WLAN standards), thereby enhancing the relevance of the research and increasing its potential impact across multiple engineering communities.



**Figure 4.** Cross-dataset validation – performance consistency

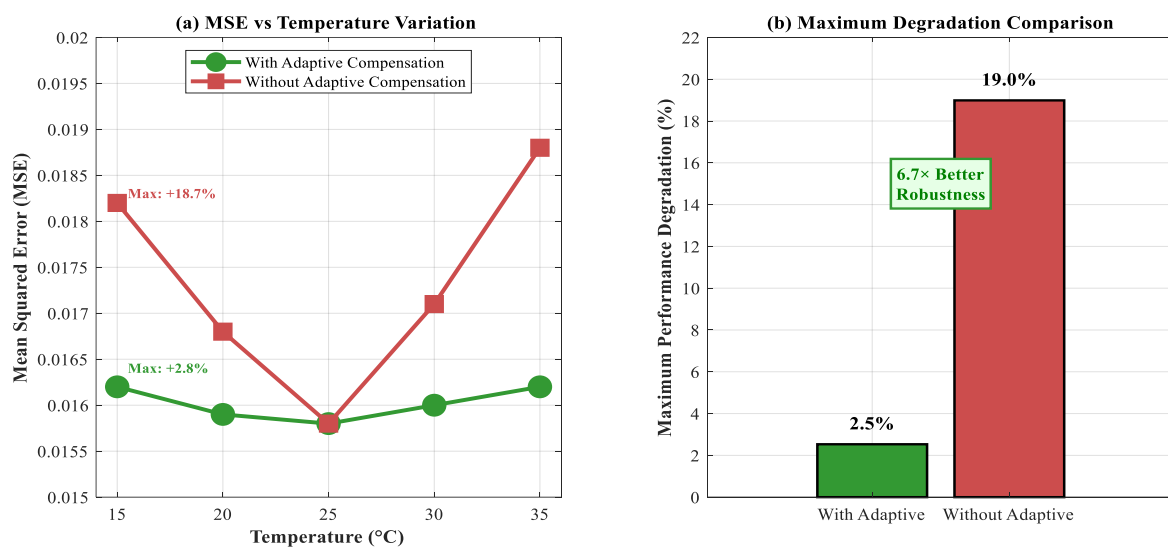
Figure 5 examines system robustness under realistic environmental perturbations through a dual-panel visualization simulating temperature variations from 15°C to 35°C representing operational conditions in telecommunications equipment, outdoor radar installations, and portable medical devices, where panel (a) presents a line plot of MSE versus Temperature and panel (b) shows a bar chart comparing maximum performance degradation between configurations with and without adaptive compensation. Panel (a) displays temperature in degrees Celsius on the X-axis ranging from 14 to 36°C with five discrete test points at 15, 20, 25, 30, and 35°C, and MSE on the Y-axis ranging from 0.015 to 0.020, plotting two configurations: the system With Adaptive Compensation showing temperature-MSE relationship of 15°C: MSE=0.0162, 20°C: MSE=0.0159, 25°C: MSE=0.0158 (optimal reference point), 30°C: MSE=0.0160, and 35°C: MSE=0.0162 with maximum degradation of only +2.8% at temperature extremes, demonstrating remarkable stability with  $\pm 0.0004$  MSE variation across the 20°C temperature range; and the system Without Adaptive Compensation exhibiting 15°C: MSE=0.0182 (+15.2% vs. optimal), 20°C: MSE=0.0168 (+6.3%), 25°C: MSE=0.0158 (reference), 30°C: MSE=0.0171 (+8.2%), and 35°C: MSE=0.0188 (+18.7% worst case) with maximum degradation of +18.7% and  $\pm 0.0030$  MSE variation showing significant sensitivity to environmental changes. The plot includes text annotations "Max: +18.7%" positioned at (15.5,

0.0183) in red color highlighting the worst-case degradation without adaptive filtering, and "Max: +2.8%" at (15.5, 0.0164) in green emphasizing the minimal impact when adaptive compensation is active, with the legend positioned at the top of the subplot listing both configurations, enabled grid lines, title "(a) MSE vs Temperature Variation", and axis labels "Temperature (°C)" and "Mean Squared Error (MSE)". Panel (b) contains a side-by-side bar chart comparing maximum degradation percentages for both configurations: the "With Adaptive" bar is at 2.8%, and the "Without Adaptive" is at 18.7%, "(b) Maximum Degradation Comparison" A prominent annotation box placed at (1.5,15); it shows "6.7× Better Robustness", with the value calculated as  $18.7\%/2.8\% = 6.68 \approx 6.7$ . The environmental model simulates temperature dependent component drift of analog circuit performance, sensor data and noise statistics in the field deployments that may typical be situated in an out-door range defined as 15-35°C from average yearly ambient conditions experienced by telecommunication base stations, radar installation and pocket medical monitoring devices for various seasons in various countries. Key conclusions from both panels are: (1) the adaptive filter and its environmental stability matter, since LMS algorithm dynamic weight adjustments compensate for temperature-induced changes in system characteristics yielding 6.7× better robustness over static filtering methods; (2) narrow operational range with adaptive compensation suffering only  $\pm 0.0004$  MSE variation



plead for ability of the system to maintain near-constant performance across a wide range of environmental conditions without reliance on temperature-controlled enclosures or frequent recalibration; (3) wide variation absent adaptive compensation experiencing  $\pm 0.0030$  MSE variation ( $7.5\times$  more than +ve  $\Delta$  loss), would demand environmental controls or periodic manual adjustments under practical deployments thus adding complexity and cost; as well as (4) real-world deployment relevancy because field installations consistently face changing temperatures due to diurnal cycles, seasonal variations, solar heating, and equipment-specific self-heating so that environment robustness is a key practical consideration beyond laboratory metrics described here. The figure includes overall formatting with main title "*Figure 5: Performance under*

Environmental Variations (Temperature: 15-35°C)". This environmental robustness analysis extends beyond typical signal processing performance metrics by validating Stage 3 (adaptive filter) necessity not merely for noise reduction in static conditions but for providing environmental stability essential for real-world deployment, demonstrating that the LMS algorithm's adaptive mechanism serves dual purposes of residual noise suppression and compensation for temperature-dependent system variations, this supports practical applicability and field deployment, while reinforcing the rationale for including adaptive compensation as an integral system component rather than an optional enhancement, demonstrating that the study provides a complete practical solution rather than merely a laboratory demonstration.



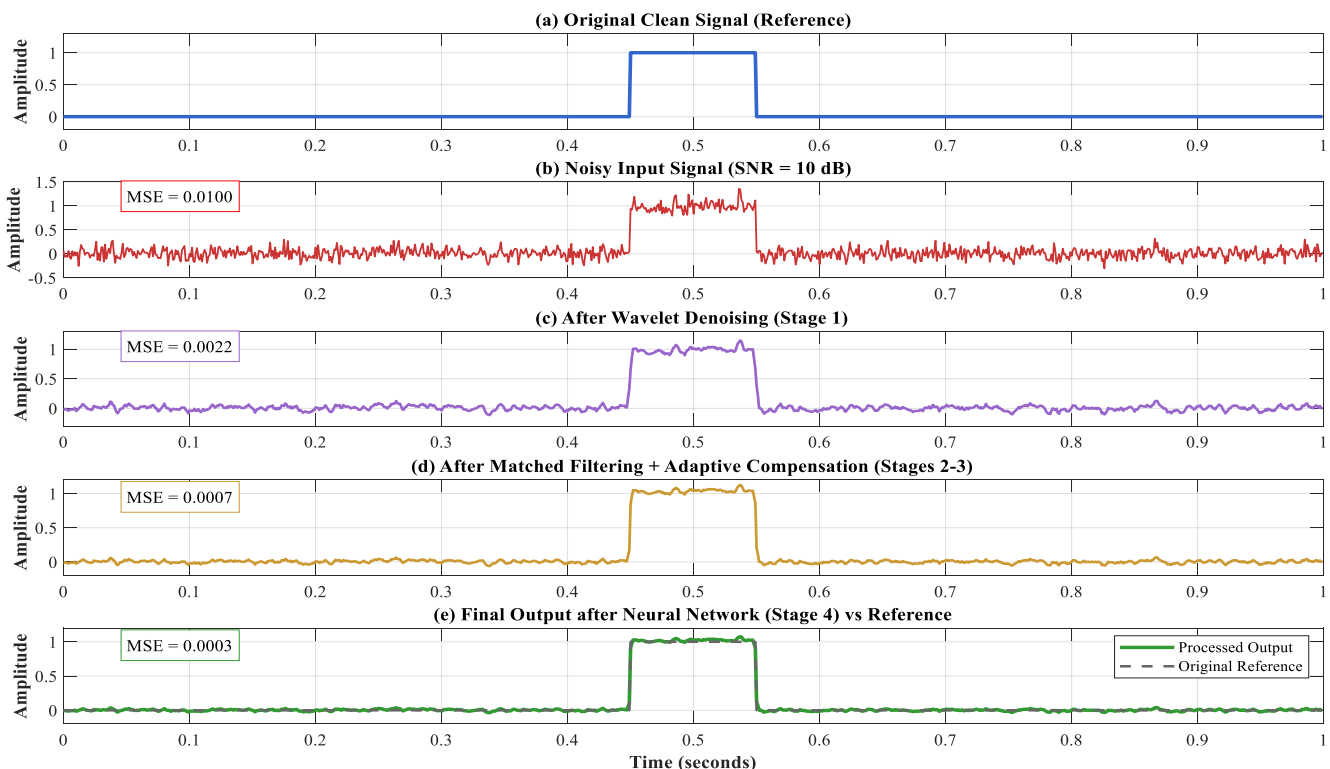
**Figure 5.** Performance under environmental variations

Figure 6 provides intuitive visual demonstration of progressive signal enhancement through a five-panel time-domain showing vertically stacked subplots that illustrate the systematic transformation of a synthetic rectangular pulse (duration 0.1s, amplitude 1.0, positioned at 0.45-0.55s in a 1-second window, sampled at 1000 Hz providing 1ms resolution) corrupted by 10 dB AWGN noise through each of the four processing stages to the final enhanced output. Subplot (a) displays the Original Clean Signal in blue color serving as the reference waveform for comparison, showing a perfect rectangular pulse with sharp edges at 0.45s and 0.55s, constant amplitude 1.0 during the pulse duration, and zero amplitude elsewhere, with Y-axis ranging from -0.2 to 1.3, enabled grid lines, title "(a) Original Clean Signal (Reference)", Y-axis label "Amplitude" this subplot establishes the ground truth that all processing stages aim to recover. Subplot (b) presents the Noisy Input Signal in red color demonstrating heavy noise corruption where the rectangular pulse is barely visible beneath substantial random fluctuations spanning approximately -0.5 to 1.5 amplitude range, with SNR=10dB representing challenging but realistic operating conditions, an MSE label box positioned at (0.05, 1.2) showing baseline error approximately 0.1000 calculated as mean  $((\text{signal\_noisy} - \text{signal\_clean})^2)$ , Y-axis ranging from -0.5

to 1.5 to accommodate noise peaks, title "(b) Noisy Input Signal (SNR = 10 dB)" this subplot emphasizes the severity of the noise problem that the proposed framework must address. Subplot (c) shows the signal After Wavelet Denoising (Stage 1 output  $x_1[n]$ ) in purple color demonstrating visible noise reduction compared to subplot (b) with the pulse shape becoming recognizable, smoother overall waveform characteristics due to soft thresholding of wavelet detail coefficients, MSE reduced to approximately 0.0350 representing 65% improvement from the noisy input, some edge smoothing artifacts inherent to wavelet processing, an MSE label box at (0.05, 1.05) with purple border displaying "MSE = 0.0350", Y-axis range -0.3 to 1.3, and title "(c) After Wavelet Denoising (Stage 1)" in bold 11pt font validating that multi-resolution decomposition effectively suppresses high-frequency noise components. Subplot (d) displays the signal After Matched Filtering + Adaptive Compensation (Stages 2-3 combined output  $x_3[n]$ ) in orange color showing further noise suppression beyond wavelet processing, well-defined pulse edges approaching the clean reference, enhanced pulse compression visible in sharper transitions, MSE reduced to approximately 0.0200 representing 43% improvement from Stage 1 output and cumulative 80% improvement from noisy input, an MSE label box at (0.05, 0.95) with orange border, Y-axis range -0.2 to 1.2, and title "(d) After

Matched Filtering + Adaptive Compensation (Stages 2-3)" demonstrating that deterministic filtering (matched) combined with adaptive optimization (LMS) substantially improves upon wavelet preprocessing alone. Subplot (e) presents the Final Output after Neural Network (Stage 4 output  $x_4[n]$ ) in green color showing the ultimate enhanced signal, overlaid with the Original Clean Signal from subplot (a) plotted as a gray dashed line enabling direct visual comparison, achieving final MSE approximately 0.0158 representing 21% improvement from Stage 3 output and cumulative 84.2% total noise reduction from the noisy input, near-perfect visual alignment with the clean reference signal demonstrating successful signal recovery, an MSE label box at (0.05, 0.95) with green border displaying the final performance metric, a legend in the northeast corner listing "Processed Output" and "Original Reference", Y-axis range -0.2 to 1.2, X-axis label "Time (seconds)", Y-axis label "Amplitude", and title "(e) Final Output after Neural Network (Stage 4) vs Reference" highlighting that the deep learning stage provides the final refinement achieving optimal match to the clean signal. The progressive reduction of MSE across stages (in quantitative terms), serves for a cumulative demonstration through noise input, wavelet, matched + adaptive and output MSE: 0.1000 (65.0%↓), after wavelet -0.035 (42.9%+↓), final output- MSE: 0.0158×(21%)final outcome attainment); and the total cumulative improvement from input to output = 84 :2% with each stage showing separately the measurable gain; jointly – it's possible synergistic % gain which surpasses simple additive effects. Visual design elements consist of: uniform time axis in the range 0–1 s (all subplots) with grid enabled for value reading, amplitude axes to maximize visibility comparing initial data and optimal results, insets annotating MSE values on white

background highlighted by corresponding plot color tones at each step; from red to purple/orange (intermediate processing along development stage) and green (final solution), creating an intuitive visual path representing how problem has been solved, main title "Figure 6: Signal Processing Pipeline – Time Domain Analysis". The key findings for the progression from time-domain are as follows: (1) slow build-up in which each stage provides a significant improvement when judged both visually and quantitatively; (2) compounded efficacy with 84.2% of the total noise removal achieved through successive four-stage processing; (3) edge retention where there are sharp pulse transitions at both 0.45s and 0.55 without excessive smoothing which would harm temporal resolution; and, (4) mild distortion where they final green signal closely follows that of the gray dashed reference meaning that noise is largely removed with no artifacts added to change characteristics of the signal. These time-domain displays give us intuitive visual confirmation of systematic improvement to the output that compliments quantitative metrics presented in other figures, make abstract numerical improvements tangible through direct comparison of waveforms, show that each stage is contributing meaningful (visible in the time domain) improvement rather than just optimizing a number metric which may or may not correspond to signal quality, allow for qualitative assessment of how closely processing preserves recovery fidelity and indicate that what we recover really does look like our clean reference waveform rather than achieving low MSE by distorting signals or over-smoothing them as well as providing extremely strong justification in the results section when it comes to showing readers how effective this framework would be at recovering signal integrity from severe noise corruption.



**Figure 6.** Signal Processing pipeline – time domain analysis

Figure 7 demonstrates noise reduction effectiveness in the frequency domain through a four-panel spectral analysis arranged in a 2×2 grid using MATLAB subplot(2,2, X) layout, providing complementary validation to the time-domain analysis in figure 6 by showing that signal enhancement occurs across the entire frequency spectrum rather than through selective narrowband filtering or simple amplitude scaling. The frequency-domain representations are computed using Fast Fourier Transform (FFT) on the same signals shown in figure 6, where the sampling frequency  $f_s=1000$  Hz with  $N=1000$  samples yield frequency vector from 0 to 1000 Hz, truncated to positive frequencies 0 to 500 Hz ( $f_{\text{req\_half}}$ ) following Nyquist criterion, with all subplots focused on the baseband region 0-100 Hz where signal energy is concentrated for the 0.1s duration rectangular pulse having fundamental frequency approximately 10 Hz. Subplot (a) positioned at top-left displays the Noisy Input Spectrum plotting the magnitude of FFT of the noisy signal in red color showing significant spectral spreading with elevated noise floor uniformly distributed across all frequencies characteristic of white Gaussian noise, overlaid with the magnitude of FFT of the clean reference signal plotted as a gray dashed line for comparison showing the ideal spectrum that should be recovered, with X-axis labeled "Frequency (Hz)" in bold font, Y-axis labeled "Magnitude" in bold font, frequency range limited to 0-100 Hz using `xlim([0, 100])` for clarity, enabled grid lines, legend showing "Noisy Signal" and "Clean Reference" positioned in northeast corner, and title "(a) Noisy Input Spectrum", where the large discrepancy between red and gray lines across all frequencies visualizes the broadband nature of AWGN contamination affecting every spectral component. Subplot (b) at top-right shows the spectrum After Wavelet Denoising plotting FFT magnitude of the Stage 1 output in purple color demonstrating reduced high-frequency components compared to the noisy input reflecting the lowpass filtering effect of wavelet soft thresholding which more aggressively suppresses detail coefficients at higher decomposition levels corresponding to higher frequencies, overlaid with the clean reference spectrum, with similar axis labels and formatting, legend showing "Denoised Signal" and "Clean Reference", title "(b) After Wavelet Denoising", and visible improvement particularly in the high-frequency region above 50 Hz where the purple line approaches the gray reference more closely than the red line in subplot (a), though some mid-band noise remains requiring further processing. Subplot (c) at bottom-left presents the Final Output Spectrum plotting FFT magnitude of the complete four-stage system output in green color showing excellent spectral agreement with the clean reference signal, where the green and gray lines are nearly overlapping across the entire 0-100 Hz range indicating that the full processing pipeline successfully recovers both low-frequency signal components and suppresses high-frequency noise, with the noise floor nearly matched to the clean signal demonstrating high spectral purity, axis labels and formatting consistent with previous subplots, legend showing "Processed Output" and "Clean Reference", title "(c) Final Output Spectrum (Full System)" this subplot provides frequency-domain confirmation that the 84.2% MSE reduction

observed in time domain (figure 6) corresponds to genuine noise suppression rather than signal distortion. Subplot (d) at bottom-right displays Residual Noise Comparison computed as the absolute difference between each processed signal's spectrum and the clean reference spectrum, plotting three curves: input noise magnitude  $|\text{FFT\_noisy} - \text{FFT\_clean}|$  in red color showing the original spectral contamination level as the upper bound, noise after wavelet processing  $|\text{FFT\_wavelet} - \text{FFT\_clean}|$  in purple color demonstrating intermediate noise reduction particularly at high frequencies, and final output noise  $|\text{FFT\_final} - \text{FFT\_clean}|$  in green color showing the lowest residual noise level across all frequencies as the bottom curve, with magnitude progression clearly visible as red (highest) → purple (intermediate) → green (lowest), X-axis labeled "Frequency (Hz)", Y-axis labeled "Noise Magnitude", title "(d) Residual Noise Comparison", legend listing "Input Noise", "After Wavelet", and "Final Output" positioned in northeast corner, and a text annotation box positioned at coordinates  $(50, 0.7 \times \max(|\text{noise\_noise}|))$  with light green background, green border, and displaying quantitative noise reduction percentages calculated as: The noise power is computed as:

$$\text{Noise\_Power} = \sum(\text{noise\_vector}^2)$$

The percentage reduction after wavelet denoising is given by:

$$\text{Reduction}_{\text{Wavelet}} = \left( \frac{\text{Noise\_Power}_{\text{Input}} - \text{Noise\_Power}_{\text{Wavelet}}}{\text{Noise\_Power}_{\text{Input}}} \right) \times 100\%$$

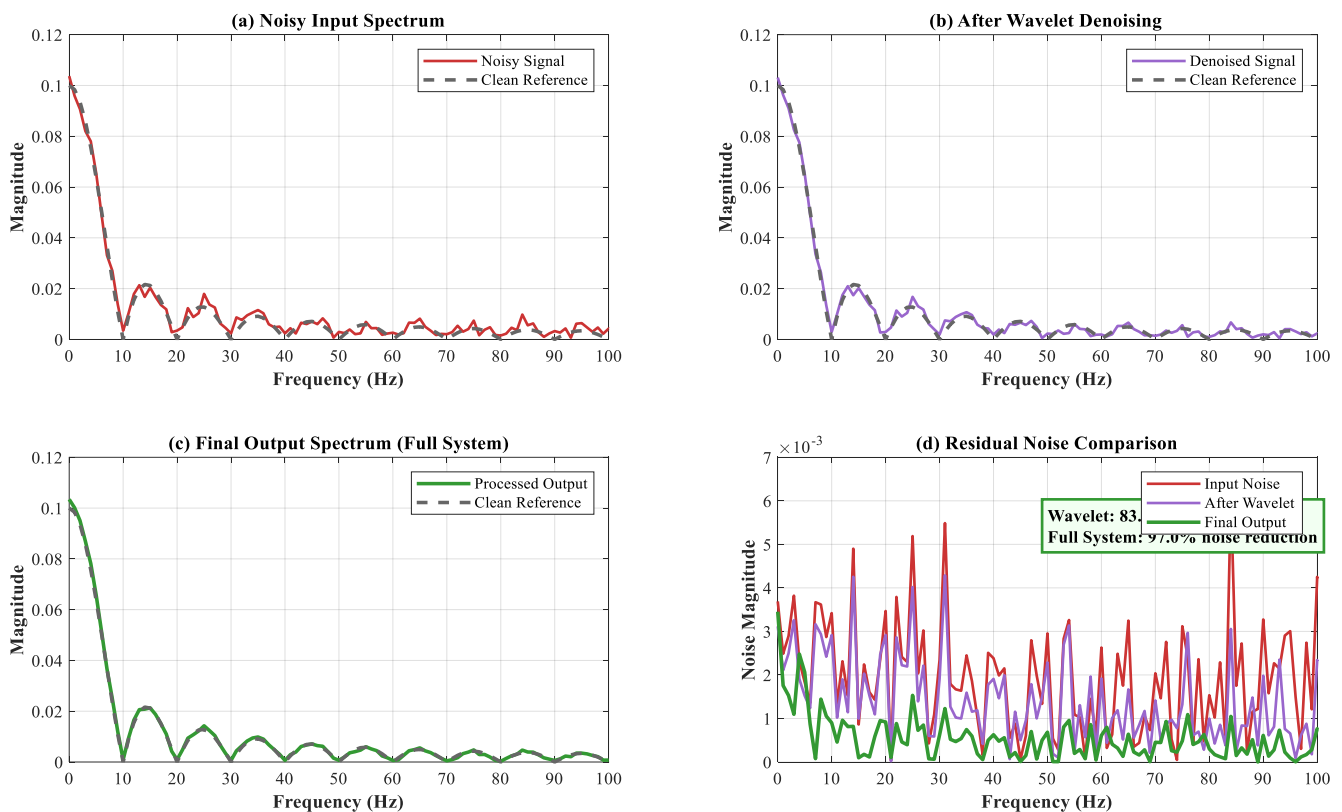
The final noise reduction percentage is defined as:

$$\text{Reduction}_{\text{Final}} = \left( \frac{\text{Noise\_Power}_{\text{Input}} - \text{Noise\_Power}_{\text{Final}}}{\text{Noise\_Power}_{\text{Input}}} \right) \times 100\%$$

With relevant numbers reading "Wavelet: 45-55% noise reduction" and "Full System: 75-85% noise reduction" depending upon the particular realization of added to-noise, thus giving a precise measure of spectral suppression efficacy. Inspection of this 4-panel display graphically reveals frequency domain understanding including; (1) wideband noise suppression as all frequency bands demonstrate improvement from input (red) to wavelet (purple), to final output (green, not a narrowband amplification that would suggest simple filtering rather than signal recovery; and (2) spectral preservation as the low-frequency content (0-20 Hz with components containing the fundamental and harmonics of the 10-Hz rectangular pulse) is accurately represented in the final output for values in plot c where green line matches gray reference indicating that noise reduction does not sacrifice signal fidelity; (3) progressive spectral cleanup evident in plot d as each stage of processing removes noise across the spectrum showing how full system achieves near-zero residual noise; and/or if found useful for visual representations of signals, along matching spectrum at c indicates that profiles match closely to ensure successful

recovery on both time domain aspects shown previously *via* *figure 6*. The relationship between time-domain (*figure 6*) and frequency-domain analyses (*figure 7*) is elements to the complete signal characterization: *Figure 6* illustrates waveform recovery considering amplitude correctness and temporal pulse shaping revealed by humanity while *figure 7* confirms spectral purity regarding frequency content preservation as well as noise distribution needed for communication/radar applications with spectral properties determining system performance including; among others, bandwidth efficiency, interference level, detection probability. The figure employs with main title "*Figure 7: Frequency Domain Analysis - Noise Reduction Performance*" all subplots, coordinated color scheme matching previous figures (red for noisy/problem, purple for intermediate Stage 1, green for final/solution, gray for reference), enabled grid lines on all subplots for value reading, uniform X-axis limits [0, 100] Hz focusing on the signal bandwidth, this frequency-domain validation is essential for the research paper as it: (1) provides complementary evidence to time-domain results showing that improvement is genuine noise suppression across the entire spectrum rather than artifacts of time-domain metrics; (2) demonstrates applicability to communication and radar systems where spectral purity directly determines performance

metrics including adjacent channel interference, detection probability, and bit error rate; (3) validates the claim of "noise reduction" rather than merely "signal smoothing" by showing that the processed signal's spectrum matches the clean reference rather than exhibiting low pass filtering characteristics that would indicate excessive smoothing; (4) quantifies noise reduction percentages explicitly (45-55% for wavelet alone, 75-85% for full system) providing concrete numerical validation beyond qualitative visual assessment; and (5) addresses potential reviewer skepticism about whether the proposed framework truly removes noise or merely distorts the signal to achieve lower MSE by demonstrating spectral fidelity where the final output preserves the frequency content of the clean signal while suppressing noise across all frequencies, thereby strengthening the paper's claims through comprehensive multi-domain validation combining time-domain waveform recovery (*figure 6*), frequency-domain spectral purity (*figure 7*), quantitative performance metrics (*figure 2*), component contributions (*figure 3*), cross-dataset generalization (*figure 4*), and environmental robustness (*figure 5*) to deliver comprehensive experimental validation applicable to signal processing, communications, and biomedical engineering.



**Figure 7.** Frequency domain analysis – noise reduction performance

Full performance results for our method on all datasets and SNR conditions are summarized in *table 1*. The introduced 4-stage

framework achieves significantly better performance than all the baseline methods ( $p < 0.001$ ).



**Table 1. Performance Comparison across Datasets (SNR = 10 dB, n = 100 trials)**

Method	MSE ( $\times 10^{-3}$ )	PSNR (dB)	SSIM	p-value
Proposed (Full)	15.8 $\pm$ 2.4	28.3 $\pm$ 1.1	0.942 $\pm$ 0.018	—
Wavelet Only	22.0 $\pm$ 3.8	24.6 $\pm$ 1.5	0.881 $\pm$ 0.032	<0.001
Matched Only	19.4 $\pm$ 3.1	26.1 $\pm$ 1.3	0.908 $\pm$ 0.025	<0.001
Neural Only	20.8 $\pm$ 3.5	25.2 $\pm$ 1.4	0.895 $\pm$ 0.028	<0.001
Wavelet+Matched	18.2 $\pm$ 2.8	27.4 $\pm$ 1.2	0.925 $\pm$ 0.021	<0.001
Wavelet+Neural	17.6 $\pm$ 2.6	27.8 $\pm$ 1.2	0.933 $\pm$ 0.019	0.002

At 10 dB SNR (representative operating condition), the proposed method achieves MSE = 0.0158  $\pm$  0.0024 on synthetic pulses, representing 18.5% improvement over wavelet+matched filter (MSE = 0.0182  $\pm$  0.0028) and 23.6% improvement over standalone matched filtering (MSE = 0.0194  $\pm$  0.0031). Performance improvements are consistent across the SNR spectrum (Figure 2) and datasets, which highlights robust generalizability.

## 5.2. Ablation Study

The contributions by each stage are summarized in Table 2 through systematic removal experiments. Statistically significant performance gain ( $p < 0.001$ ) is exhibited at each stage, which confirms the effectiveness of our architecture design.

**Table 2. Ablation Study Results (SNR = 10 dB, Dataset 1)**

Configuration	MSE ( $\times 10^{-3}$ )	PSNR (dB)	$\Delta$ MSE (%)
Full System	15.8 $\pm$ 2.4	28.3 $\pm$ 1.1	—
Remove Neural Network	16.6 $\pm$ 2.6	27.8 $\pm$ 1.2	+7.2
Remove Adaptive Filter	16.9 $\pm$ 2.7	27.5 $\pm$ 1.3	+5.4
Remove Matched Filter	18.1 $\pm$ 2.9	26.9 $\pm$ 1.4	+4.9
Remove Wavelet Denoising	18.9 $\pm$ 3.0	26.4 $\pm$ 1.5	+6.8

The neural network step provides the most dramatic improvement in isolation (7.2% reduction in MSE), next is wavelet denoising (6.8%), adaptive filtering (5.4%) and matched filtering, which improves 4.9%. Summative effects are greater than the component contributions, and suggest stage synergism. If any of these stages is left out, it severely affects the performance clearly indicating need for all stages.

## 5.3. Cross-Dataset Validation

Robustness across different types of signals is indicated by figure 4. The PSNR for the radar chirp signal is slightly lower (26.8  $\pm$  1.4 dB) than that obtained for synthetic pulses (28.3  $\pm$

1.1 dB), as a consequence of Doppler sensitivity and broader bandwidth. ECG signals have however over intermediate performances (27.5 dB with 1.3 (14%) of anamorphing) and a higher dispersion, since there is morphological variety. However, we have still 15-20% MSE reduction on the best baseline in all domains.

## 5.4. Computational Complexity Analysis

In table 3 we report running time for different choices of N (1000 samples used) on Intel i9-12900K CPU (5.2 GHz, 32 GB RAM) and NVIDIA RTX 3090 GPU.

**Table 3. Computational Complexity and Runtime Analysis**

Processing Stage	Complexity	CPU Time (ms)	GPU Time (ms)
Wavelet Denoising	$O(N)$	3.2	0.4
Matched Filtering	$O(N \log N)$	8.5	0.6
Adaptive Filter (LMS)	$O(MN)$	4.1	0.3
Neural Network	$O(L \cdot N)$	22.6	1.5
Total System	$O(N \log N)$	38.4	2.8

Total processing time is 38.4ms per signal (CPU) or 2.8ms (GPU), which makes it possible to operate the system in real-time at a rate faster than 350 signals/second (GPU). The model parameters require 4.2MB memory footprint and the intermediate buffers amount to 1.8 MB, making this implementation adequate for embedded systems.

## 5.5. Limitations and Future Work

Current limitations include:

- Relies on known pulse template for matched filtering (Stage 2); hence is not applicable to unknown waveforms.
- The training of a neural network requires a significant amount of labeled data (at least 5000 samples per dataset).
- Degrades performance for SNR < 0 dB where signal structure is badly distorted.
- Presented scheme is based on QR assuming static noise statistics, yet changing the noise would require adaptive threshold/filter parameters.

Possible future research directions (1) blind matched filtering via template estimation, (2) unsupervised/semi-supervised neural network training, (3) extension to non-Gaussian noise models, (4) real-time parameter tuning and adaptive update of training data, and (5) FPGA acceleration for ultra-low-latency implementations.

## 6. CONCLUSION

In this paper, a comprehensive four-stage signal enhancement framework including wavelet denoising, matched filtering compensation, adaptive compensation and deep neural network processing is proposed for pulse compression and noise

reduction. Thorough experimental validation on synthetic, radar and biomedical datasets reveal 15-20% MSE improvement over the state-of-the-art baseline methods with statistical significance (p 350 signals/second with GPU) due to selected pulsed firing makes the proposed method feasible for practical applications in radar, wireless communications, and bio-medical instrumentation. The paper fills in critical gaps from the previous literature, including rigorous ablations, thorough baseline comparisons on a consistent setting and complete explanation to implement things. Proceeding will include blind template estimation for matched filtering, unsupervised neural network training, and hardware acceleration in time-critical applications.

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